

The background of the slide is a blurred image of a computer monitor displaying financial data. On the left, there's a blue semi-transparent box containing the title. The monitor shows several windows: a 'Quote List (2)' window with columns for 'Name', 'Last', and 'Change'; a 'World Markets' window with a table of market indices; and several line charts showing price movements for various assets like EURUSD and Gold. The charts are overlaid on a grid, and the overall color scheme is dark with white and blue highlights.

PREDICTING THE FUTURE: INTRODUCTION TO REGRESSION ANALYSIS

NURULJANNAH BT NOR AZMI



What is regression analysis?

We often hear of new, complex “machine learning” methods that:

- Allow us to generate human language.
- Very accurately predict changes in the stock market.
- Recognize that an image contains a person or specific object.

What is regression analysis?



- Regression model analysis is utilized in various applications.
- Adrien-Marie Legendre introduced the concept of regression models in 1805.
- Since then, regression-based modeling has remained fundamental in applied statistics!



What is regression analysis?

Regression analysis comprises a set of statistical techniques aimed at estimating the relationship between:

Dependent variable (outcome variable)

One OR More independent variables (predictor variables)

INDEPENDENT VARIABLE

VARIABLE THAT IS CHANGED

Amount of Water



DEPENDENT VARIABLE

VARIABLE AFFECTED BY THE CHANGE

Size of Plant
Number of Leaves
Living or Dead?



When to apply Regression Analysis?

Regression analysis can address a broad range of questions, such as:

1. Is the relationship between two variables linear?
2. Which variable contributes the most to the outcome measurement?
3. How accurately can we predict future values?
4. Is our outcome variable caused by another variable?

AGE +



42 372
369 491
Start at monthly
Can we do this

AGE



Treatment methods

Length of hospital stay



Severity of illness

Estimating Coefficient(s)

Assuming we are analyzing a basic model consisting of a single predictor, one outcome variable, and one coefficient, we can formally represent this model as follows:

$$Y = \beta_0 + \beta_1 X_1 + \text{error}$$

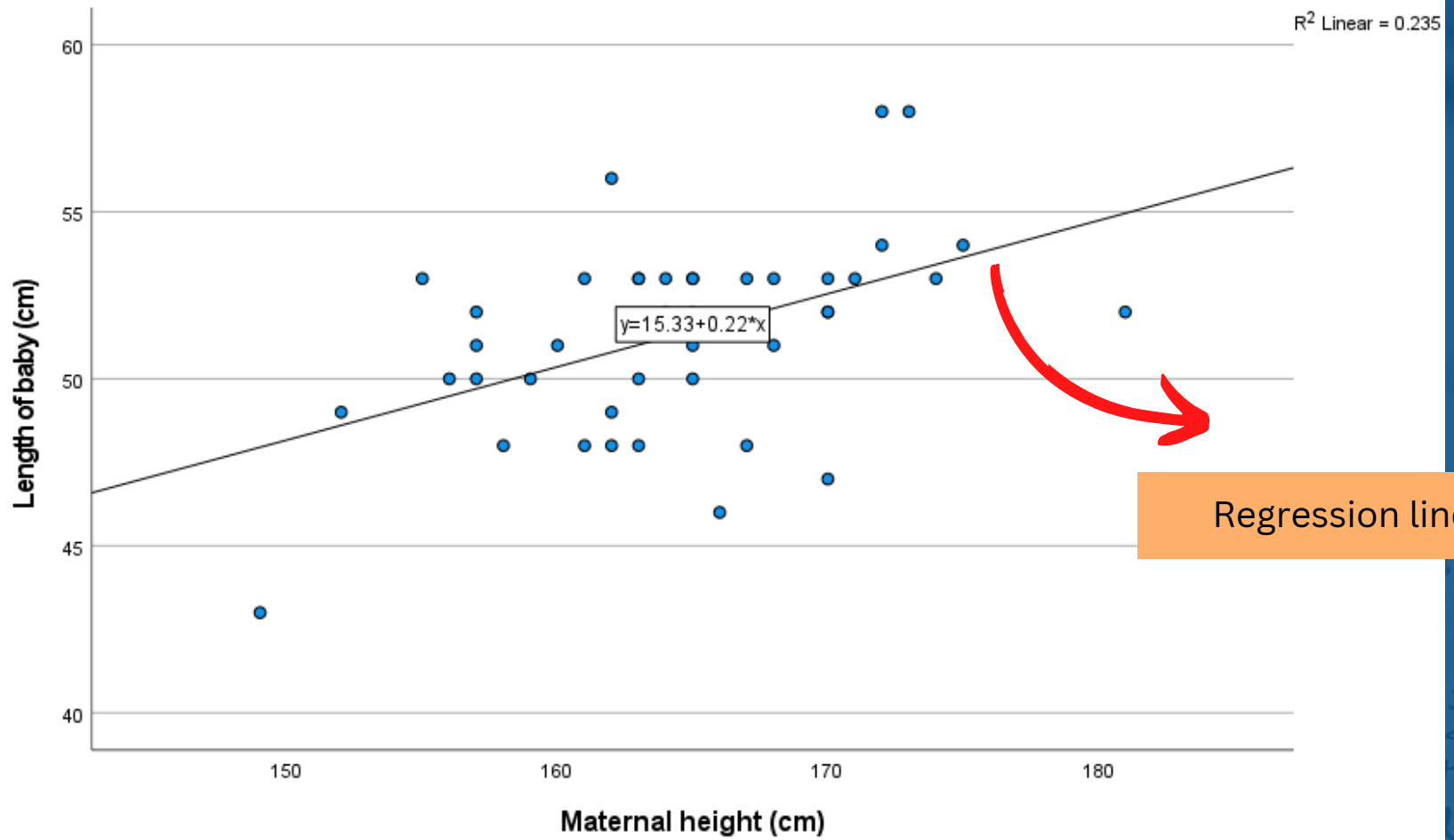
Y = outcome

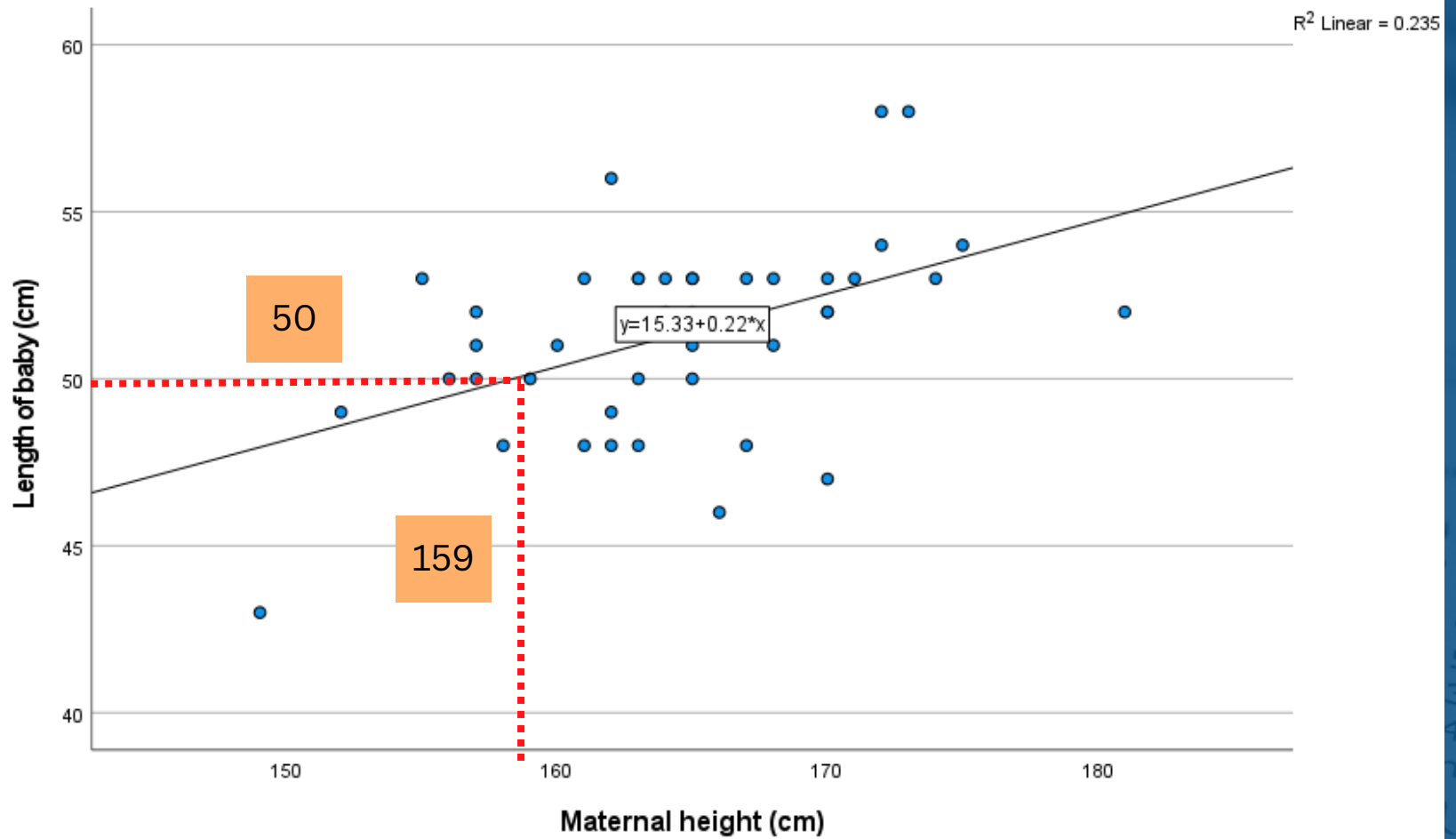
β_0 = an intercept of the regression line

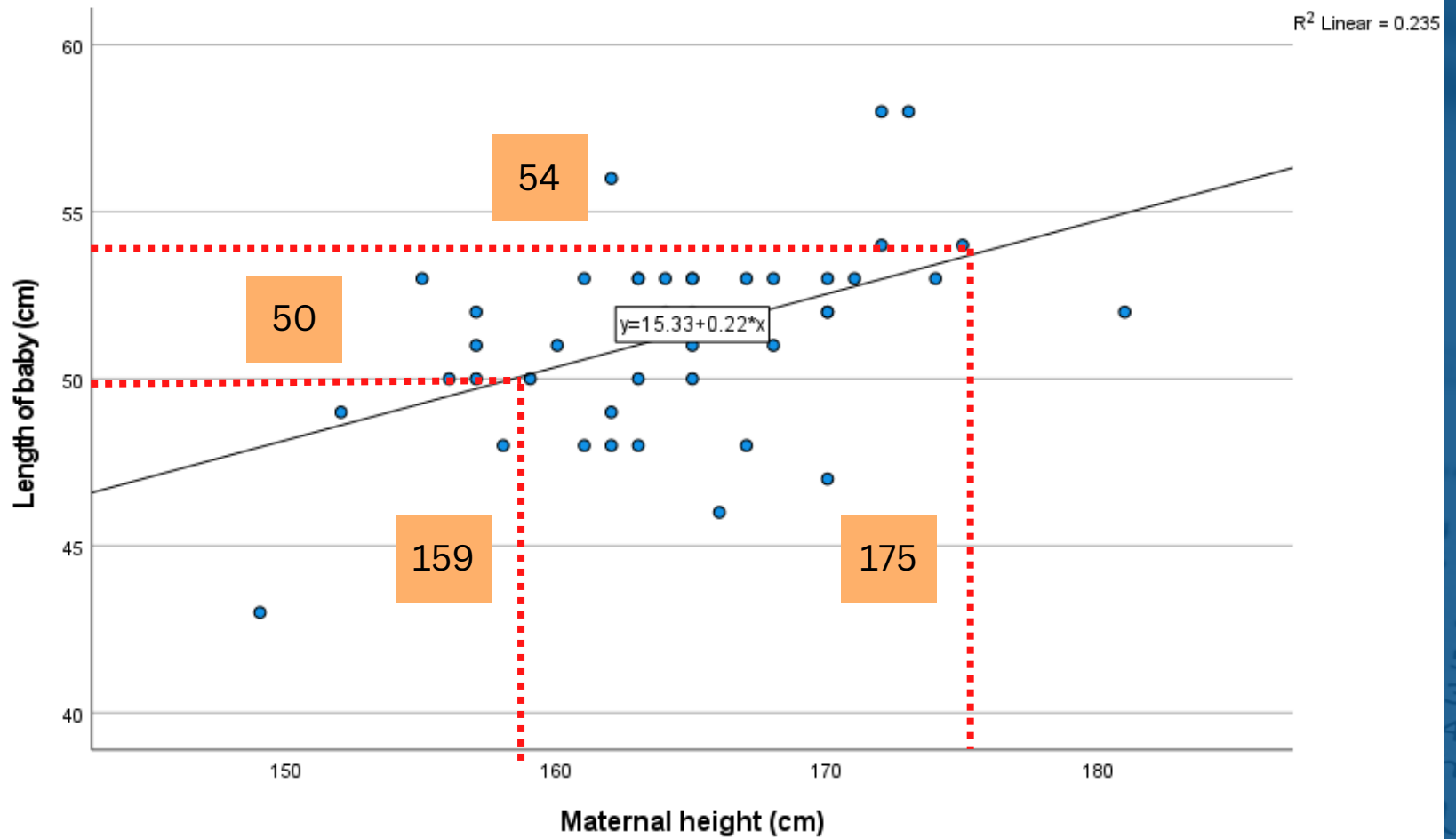
β_1 = a slope of the line / regression coefficient for independent variable

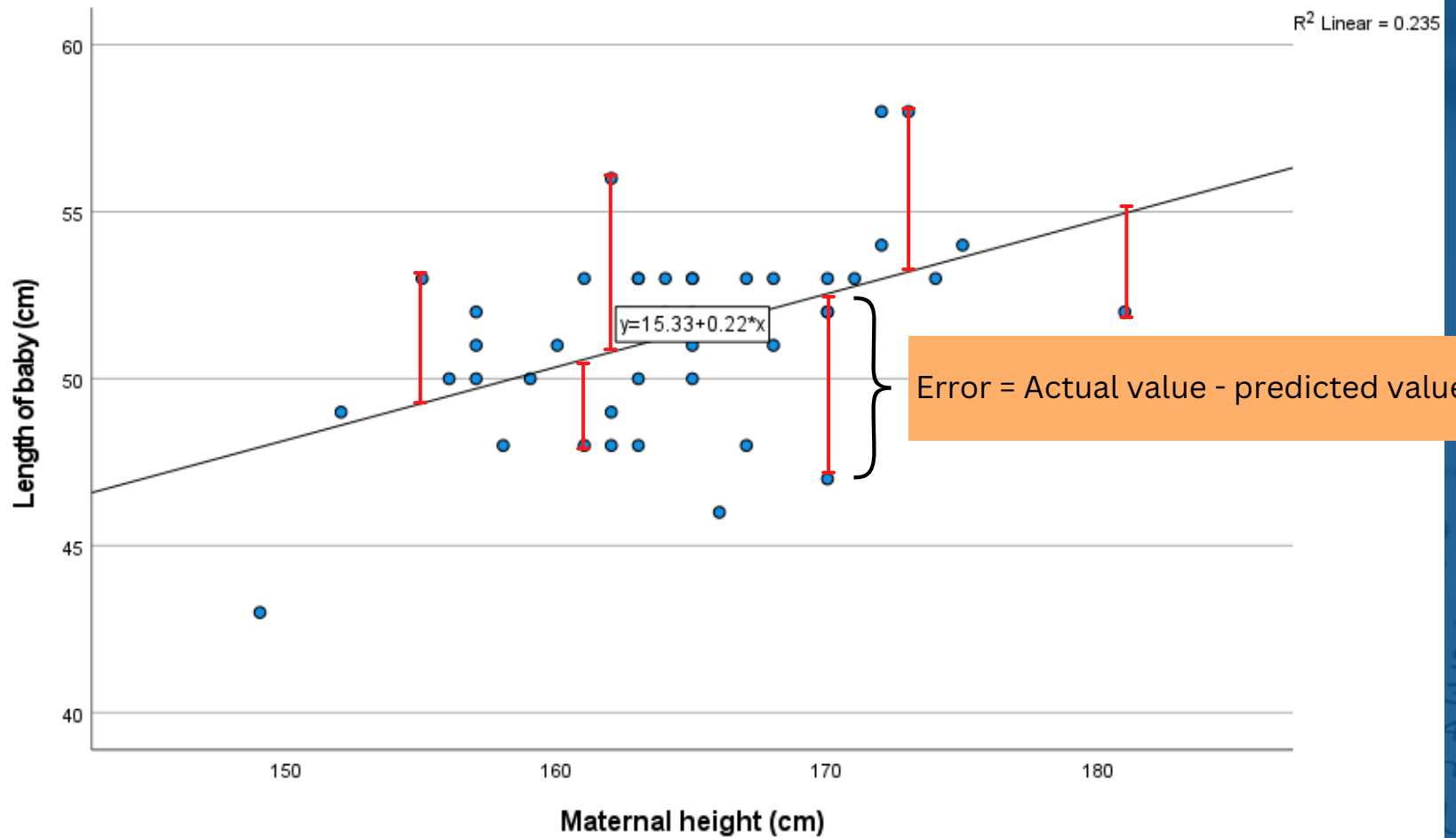
X_1 = independent variable

error = residual









SIMPLE LINEAR REGRESSION

Simple Linear Regression is used to estimate the relationship between two quantitative variables.

Dependent variable : numerical

Independent variable : numerical



When to apply Simple Linear Regression?

You can use simple linear regression when you want to identify:

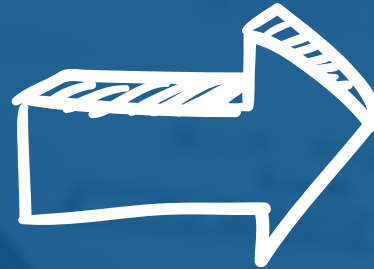
1. How strong the relationship between two variables.
2. To predict a value of one variable for a given value of the other.

How much the value Y (dependent variable) varies with one unit of change in value X (independent variable)

SIMPLE LINEAR REGRESSION - ONLY ONE INDEPENDENT VARIABLE

Independent variable (x)

Mother's height



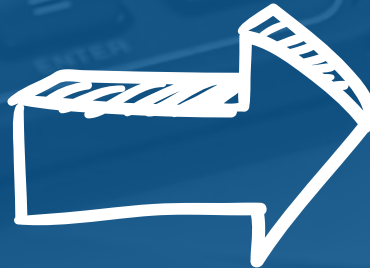
Dependent variable (y)

Length of baby

MULTIPLE LINEAR REGRESSION - MORE THAN ONE INDEPENDENT VARIABLES

Independent variables (x)

Mother's height
Mother's weight
Age



Dependent variable (y)

Length of baby

INTRODUCTION

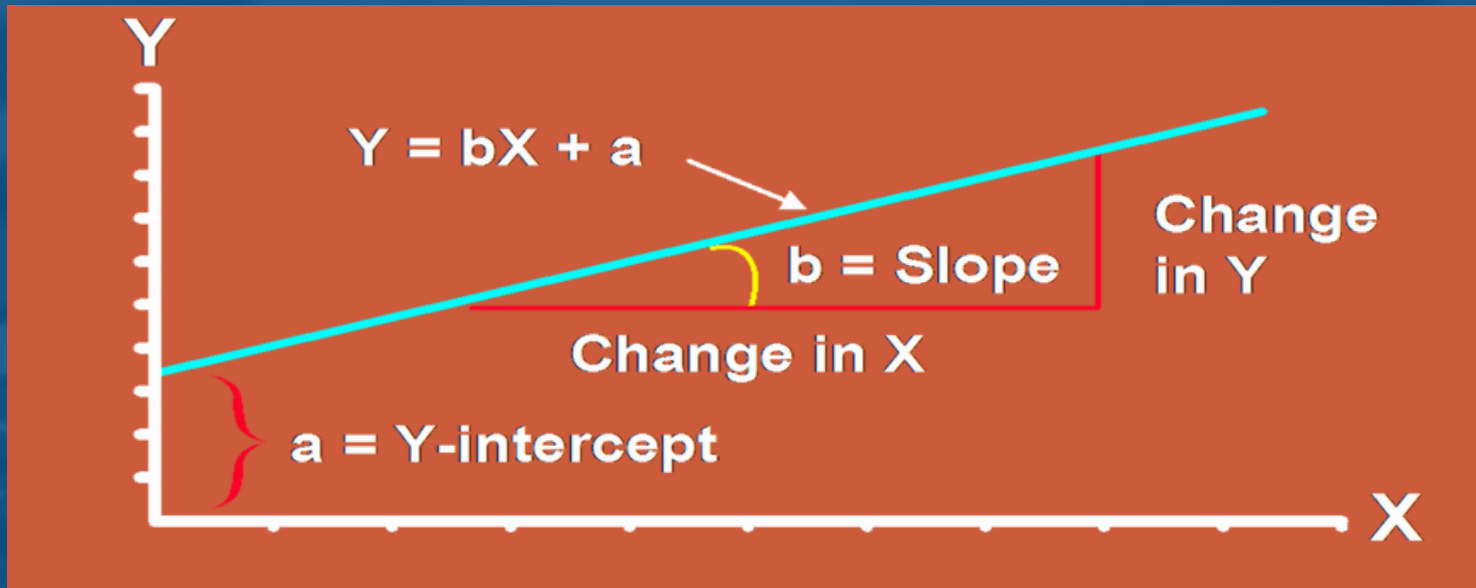
If independent variables are combination of numerical and categorical or categorical only -
General Linear Regression

Dependent (outcome) : numerical

Independent (predictor) : 2 or more combination of numerical and categorical or categorical only



Regression Equation



$$y = a + bx$$

x : independent variable

y: dependent variable

a: an intercept of the regression line (value of Y when X=0)

b: a slope of the line (an amount of change in Y for a unit change in X)

Coefficient of Determination (r^2)

- Ranges from 0 to 1.
- It provides a measure of how well future outcomes are likely to be predicted by the model.
- How much the independent of 'x' is explained by dependent 'y'.

ASSUMPTIONS OF THE MODEL

L

Relationship between the independent and dependent variable is linear.
(Linearity).

I

Independent
observation

N

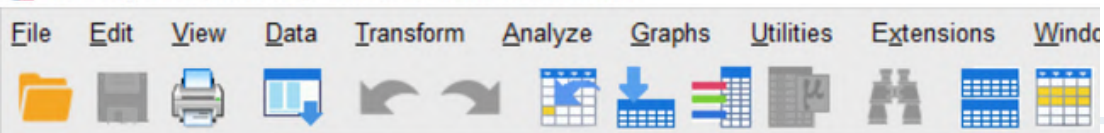
Residuals should be approximately normally distributed

E

Homoscedasticity
(Equal variances)

CHECKING MODEL ASSUMPTIONS

Assumptions	How to check?
1. Relationship between the independent and dependent variable is <u>linear</u> (<u>Linearity</u>).	Scatter plot between independent and dependent variable
2. <u>Independent</u> observation	Done during design stage
3. Residuals should be approximately <u>normally</u> distributed	Histogram with overlaid normal curve of residuals
4. Homoscedasticity (<u>Equal</u> variances)	Scatter plot between residuals and predicted values (XP - YR)



9 :

	ID	Headcirc	Length	Birthweight	Ges
1	1360	34	56	4.55	
2	1016	36	53	4.32	
3	462	39	58	4.10	
4	1187	38	53	4.07	
5	553	37	54	3.94	
6	1636	38	51	3.93	
7	820	34	52	3.77	
8	1191	33	53	3.65	
9	1081	38	54	3.63	
10	822	35	50	3.42	
11	1683	33	53	3.35	
12	1088	36	51	3.27	
13	1107	36	52	3.23	
14	755	33	53	3.20	
15	1058	34	53	3.15	
16					
17					
18					
19					
20					
21					
22					
23					
24					
25					
26					
27	431	30	48	1.92	

EXAMPLE

Open dataset:
birthweight.sav

This dataset contains information on new born babies and their parents. Is there any relationship between maternal height and length of baby?

EXAMPLE

A study was conducted to determine the relationship between mother's height and the length of baby, with the researcher aiming to **forecast** the baby's length using the mother's height as a predictor.

Mother's height

Length of baby

Numerical

Numerical

Simple Linear Regression

List down all the variables

Identify the types of variables

Identify the right statistical analysis

STEPS IN SIMPLE LINEAR REGRESSION

Step 1: State your research hypothesis

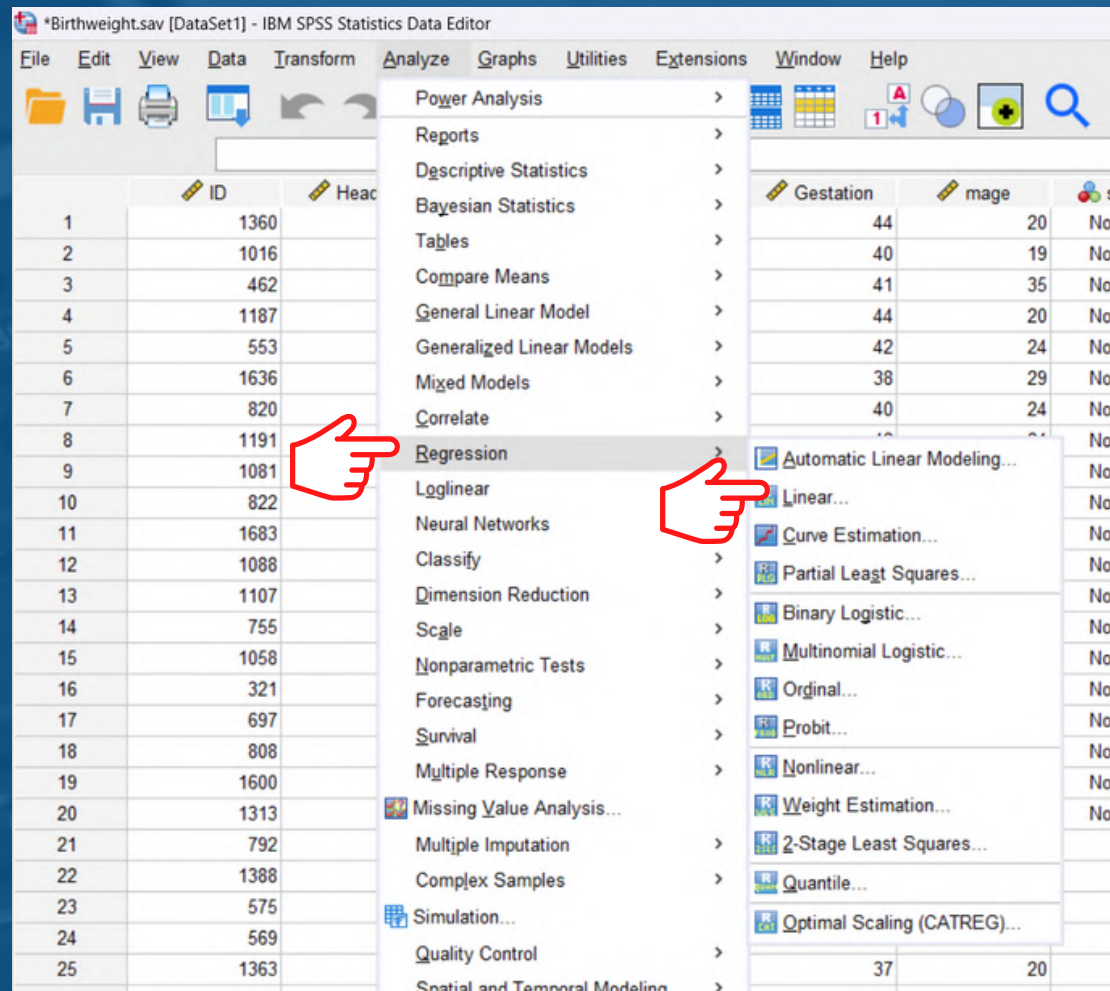
Null hypothesis and Alternative hypothesis

H_0 : There is no relationship between mother's height and the length of baby

H_A : There is a relationship between mother's height and the length of baby

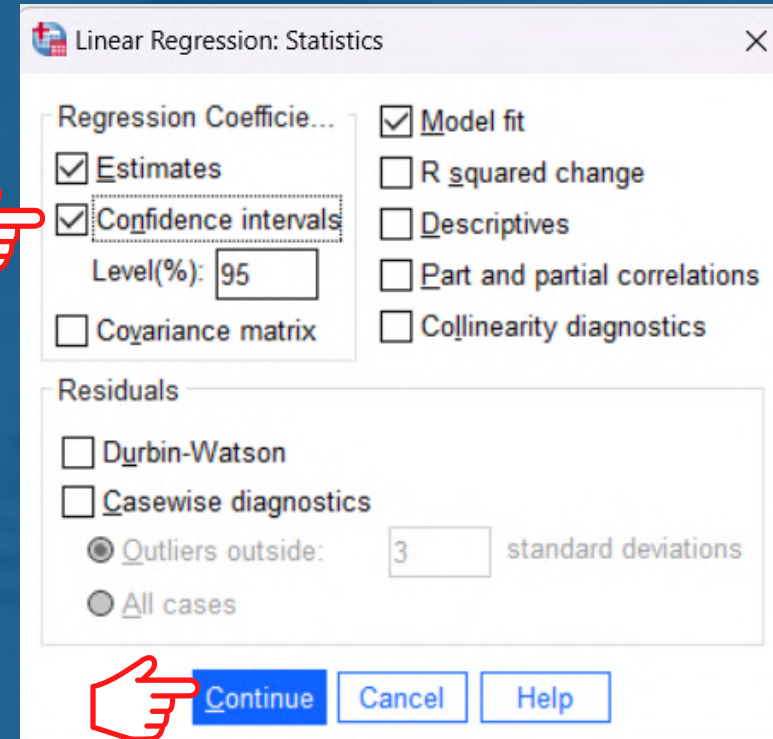
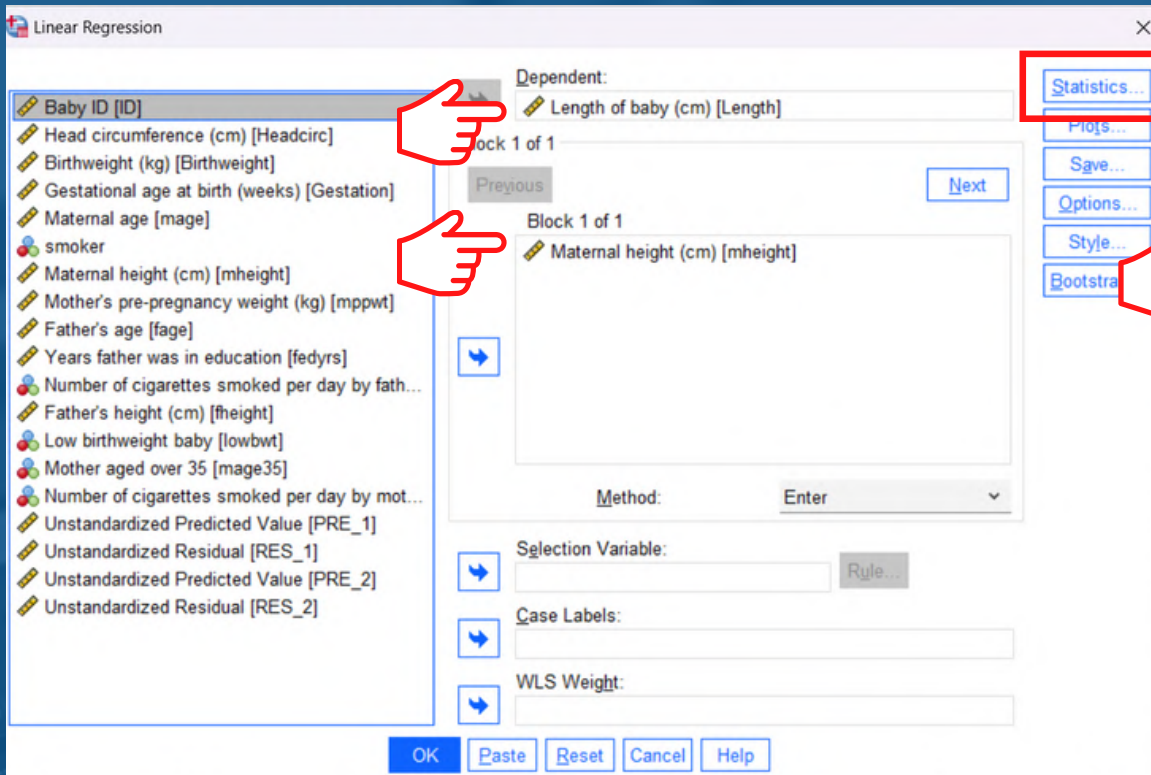
Step 2: Run Simple Linear Regression

Go to: Analyze > Regression > Linear



The screenshot shows the IBM SPSS Statistics Data Editor interface. The 'Analyze' menu is open, and the 'Regression' option is selected. The 'Linear...' option is highlighted in the submenu. Two red hand icons point to the 'Regression' and 'Linear...' options. The background shows a data table with columns 'ID' and 'Head'.

ID	Head
1	1360
2	1016
3	462
4	1187
5	553
6	1636
7	820
8	1191
9	1081
10	822
11	1683
12	1088
13	1107
14	755
15	1058
16	321
17	697
18	808
19	1600
20	1313
21	792
22	1388
23	575
24	569
25	1363



Coefficients^a

Model		Unstandardized Coefficients		Standardized	t	Sig.	95.0% Confidence Interval for B	
		B	Std. Error	Coefficients			Lower Bound	Upper Bound
1	(Constant)	15.334	10.271		1.493	.143	-5.425	36.093
	Maternal height (cm)	.219	.062	.485	3.507	.001	.093	.345

a. Dependent Variable: Length of baby (cm)

Model Summary^b

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.485 ^a	.235	.216	2.599

a. Predictors: (Constant), Maternal height (cm)

b. Dependent Variable: Length of baby (cm)

23.5% of the variation in length of baby is explained by mother's height according to the linear regression model ($r^2 = 0.235$).

ANOVA^a

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	83.110	1	83.110	12.302	.001 ^b
	Residual	270.223	40	6.756		
	Total	353.333	41			

a. Dependent Variable: Length of baby (cm)
b. Predictors: (Constant), Maternal height (cm)

This table indicates that the regression model predicts the dependent variable significantly well (refer to p-value).

Here, $p < 0.05$, which is less than 0.05, and indicates that the regression model statistically significantly predicts the outcome variable.




Result presentation for Simple Linear Regression

Table 1: Simple linear regression

Variable	SLR ^a	
	b* (95% CI)	p-value
Mother's height	0.22 (0.09,0.35)	0.001

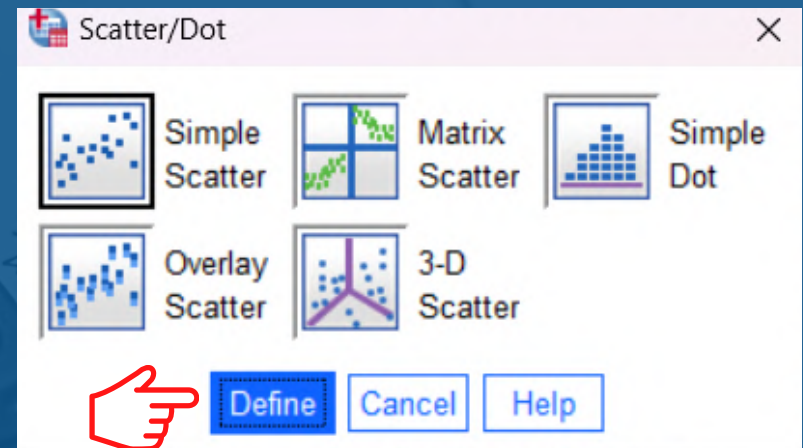
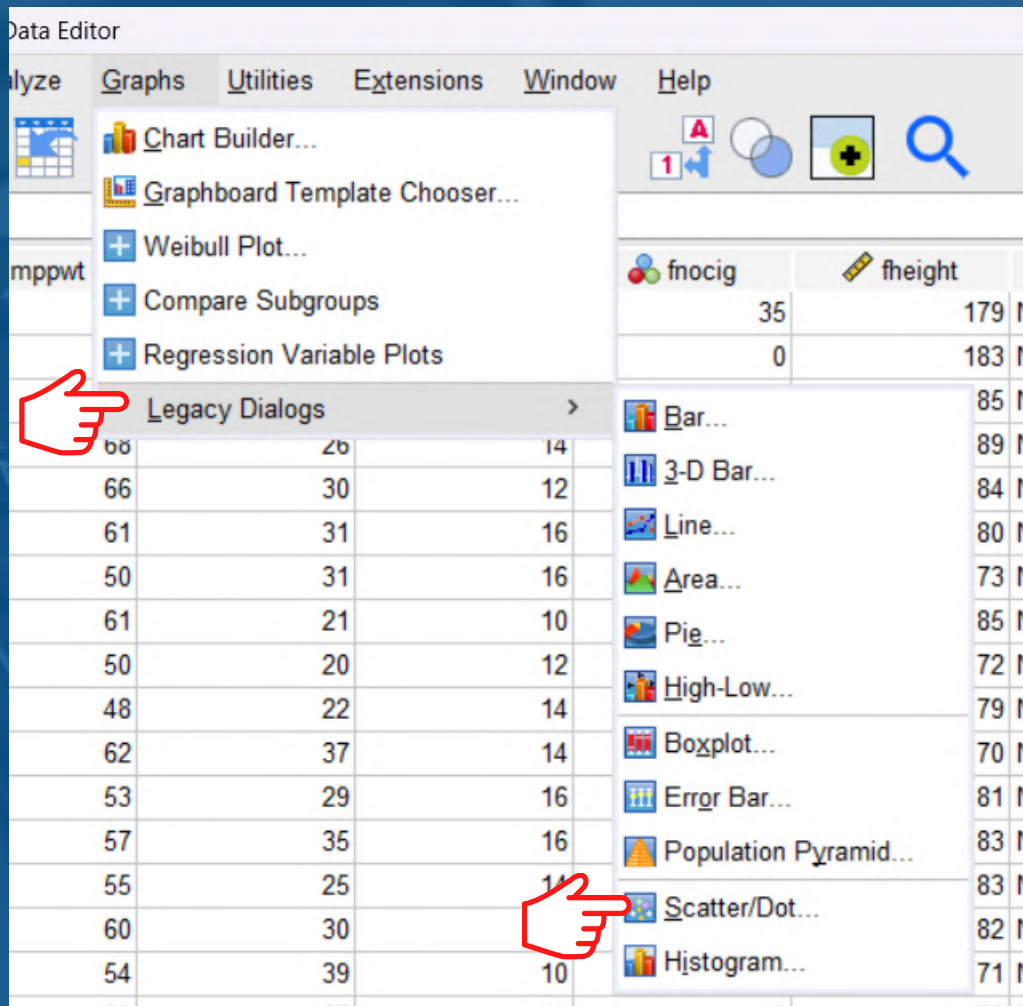
^a Simple linear regression
b* = crude regression coefficient

Step 3: Checking assumptions

Assumptions	How to check?
1. Independent observation	Done during design stage
2. Relationship between the independent and dependent variable is <u>linear</u> (Linearity).	Scatter plot between independent and dependent variable 
3. Homoscedasticity (<u>Equal</u> variances)	Scatter plot between residuals and predicted values (XP - YR) 
4. Residuals should be approximately <u>normally</u> distributed	Histogram with overlaid normal curve of residuals 

Checking assumption : Linearity

Go to: Graph > Legacy Dialogs > Scatter/Dot



Simple Scatterplot

Y Axis:
Length of baby (cm) [Length]

X Axis:
Maternal height (cm) [mheight]

Set Markers by:

Label Cases by:

Panel by

Rows:

Nest variables (no empty rows)

Columns:



Nest variables (no empty columns)

Template

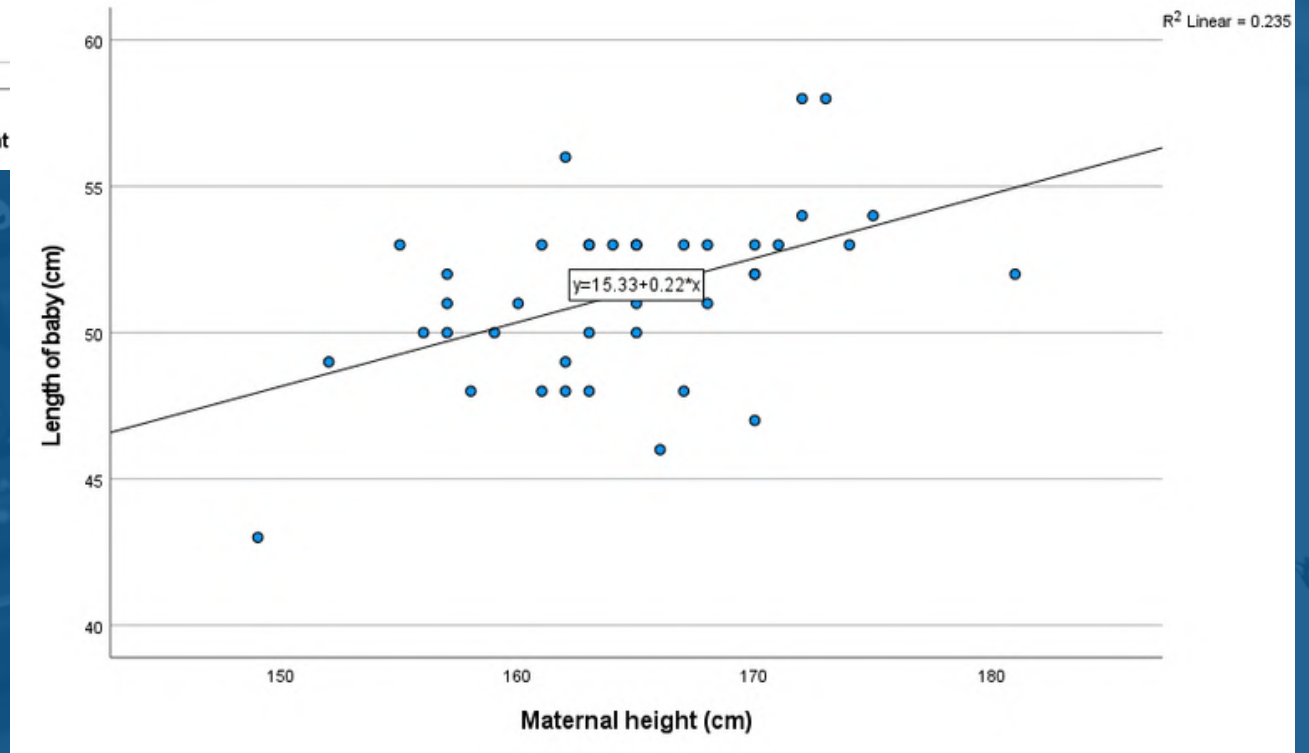
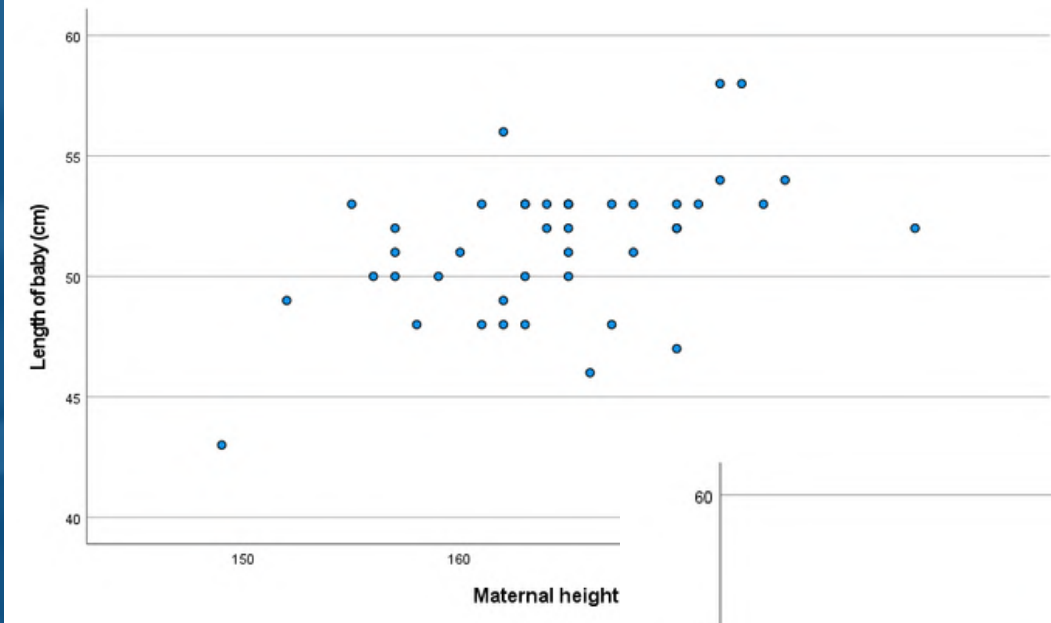
Use chart specifications from:
File...

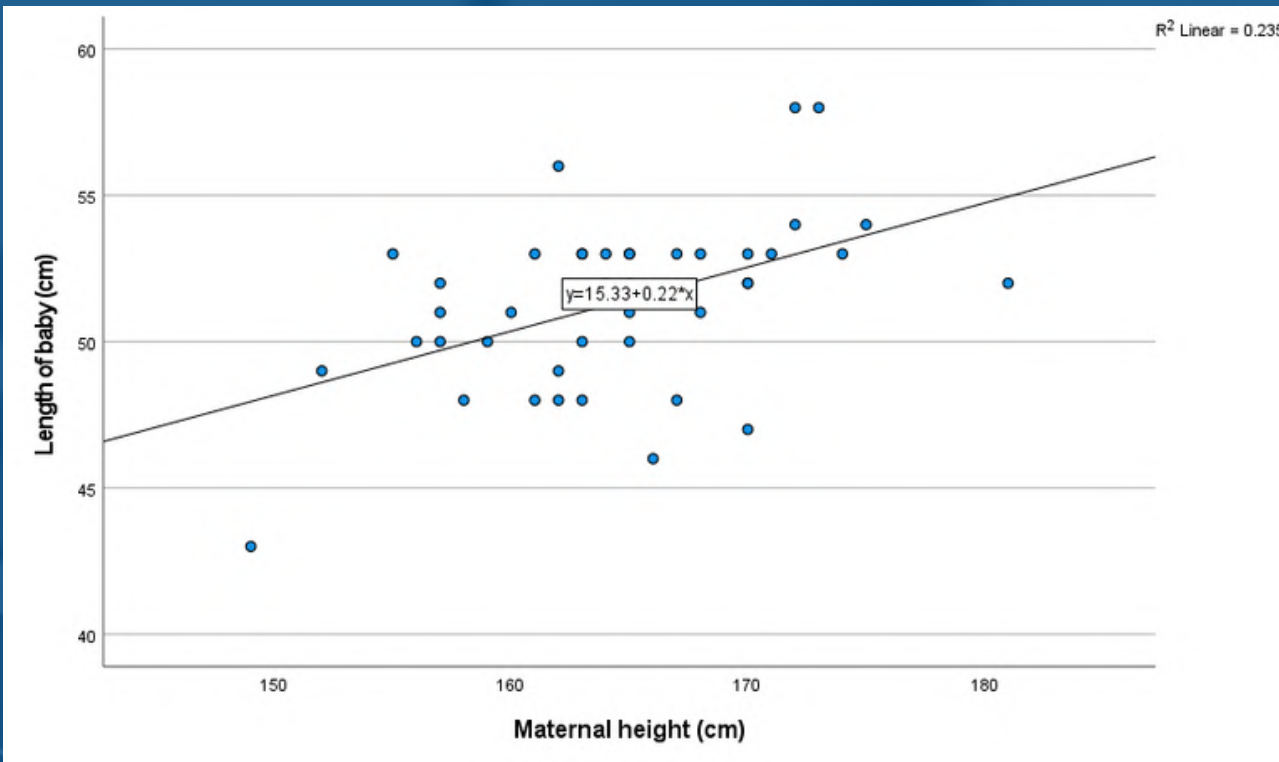
OK Paste Reset Cancel Help

Titles... Options...

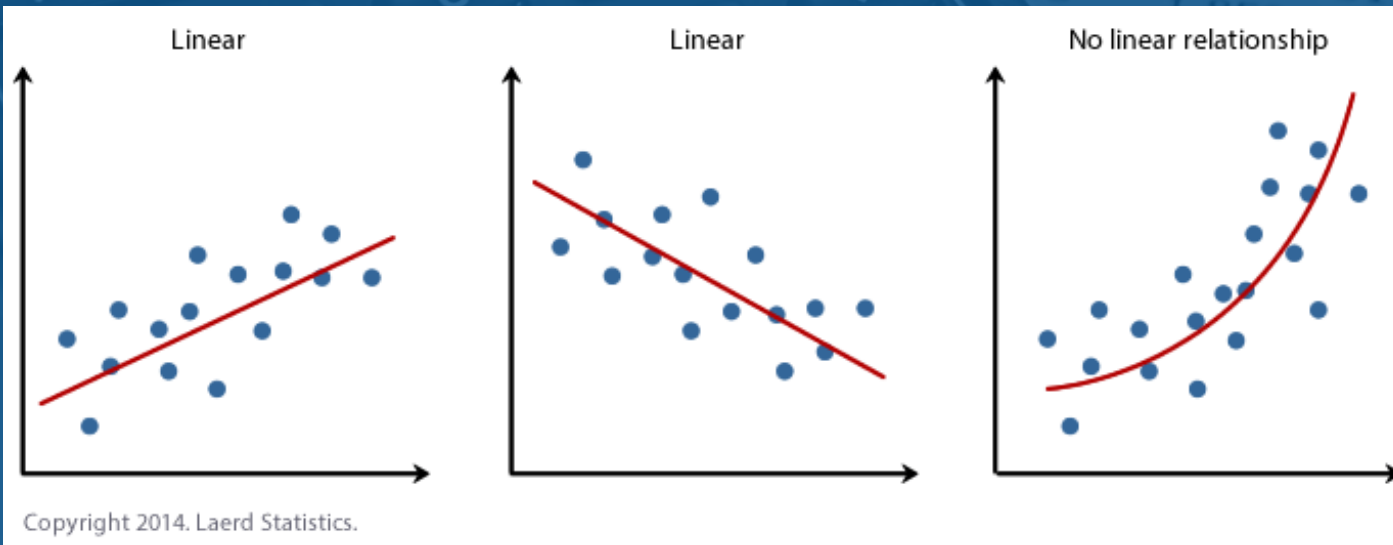


Double click the plot and click





Linear relationship of two continuous variables. Linearity assumption is met.



Example of linear and non-linear relationship

Checking assumption: Homoscedasticity (equal variances)

Go to: Analyze > Regression > Linear

The screenshot shows the IBM SPSS Statistics Data Editor interface. The 'Analyze' menu is open, and the 'Regression' option is selected. The 'Linear...' option is also selected. Two red hand icons point to these options. The background shows a data table with columns 'ID' and 'Head'.

ID	Head
1	1360
2	1016
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10	822
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13	1107
14	755
15	1058
16	321
17	697
18	808
19	1600
20	1313
21	792
22	1388
23	575
24	569
25	1363
26	300
27	431

Linear Regression

Dependent:
Length of baby (cm) [Length]

Block 1 of 1

Previous Next

Independent(s):
Maternal height (cm) [mheight]

Method: Enter

Selection Variable: Rule...




Case Labels:

WLS Weight:

Statistics...
Flags...
Save...
Options...
Style...
Bootstrap...

Baby ID [ID]
Head circumference (cm) [Headcirc]
Birthweight (kg) [Birthweight]
Gestational age at birth (weeks) [Gestation]
Maternal age [mage]
smoker
Maternal height (cm) [mheight]
Mother's pre-pregnancy weight (kg) [mppwt]
Father's age [fage]
Years father was in education [fedyrs]
Number of cigarettes smoked per day by fath...
Father's height (cm) [fheight]
Low birthweight baby [lowbwt]
Mother aged over 35 [mage35]
Number of cigarettes smoked per day by mot...

OK Paste Reset Cancel Help



Linear Regression: Save

Predicted Values

Unstandardized
 Standardized
 Adjusted
 S.E. of mean predictions

Distances

Mahalanobis
 Cook's
 Leverage values

Prediction Intervals

Mean Individual
Confidence Interval: 95 %

Coefficient statistics

Create coefficient statistics

Create a new dataset
Dataset name:

Write a new data file
File:

Export model information to XML file

Include the covariance matrix



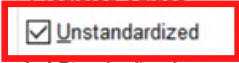
Residuals

Unstandardized
 Standardized
 Studentized
 Deleted
 Studentized deleted

Influence Statistics

DfBetas
 Standardized DfBetas
 DfFits
 Standardized DfFits
 Covariance ratios

Continue Cancel Help



Predicted value

Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.
		B	Std. Error	Beta		
1	(Constant)	15.334	10.271		1.493	.143
	Maternal height (cm)	.219	.062	.485	3.507	.001

a. Dependent Variable: Length of baby (cm)

	ID	Length	mheight	PRE_1	RES_1
1	1360	56	162	50.79650	5.20350

$$y = a + bx$$

$$\text{Length of baby} = 15.33 + (0.22 * \text{mother's height})$$

Predicted length of baby whose mother's height is 162cm is:

$$\text{Length of baby} = 15.33 + (0.22 * 162) = 50.97$$

Residuals

	ID	Length	mheight	PRE_1	RES_1
1	1360	56	162	50.79650	5.20350

The difference between the observed value of the dependent variable and the value predicted by the regression line.

Residual = observed length - predicted length

Residual = $56 - 50.8 = 5.2$

Go to: Graph > Legacy Dialogs > Scatter/Dot


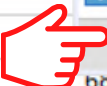
Data Editor

Analyze Graphs Utilities Extensions Window Help

Chart Builder...
Graphboard Template Chooser...
Weibull Plot...
Compare Subgroups
Regression Variable Plots
Legacy Dialogs >

	fncig	fheight	
	35	179	N
	0	183	N
			85 N
			89 N
			84 N
			80 N
			73 N
			85 N
			72 N
			79 N
			70 N
			81 N
			83 N
			83 N
			82 N
			71 N


Bar...
3-D Bar...
Line...
Area...
Pie...
High-Low...
Boxplot...
Error Bar...
Population Pyramid...
Scatter/Dot...
Histogram...



Scatter/Dot

Simple Scatter Matrix Scatter Simple Dot
Overlay Scatter 3-D Scatter

Define Cancel Help



Simple Scatterplot

Y Axis:
Unstandardized Residual [RES_1]

X Axis:
Unstandardized Predicted Value [PRE_1]

Set Markers by:

Label Cases by:

Panel by

Rows:

Nest variables (no empty rows)

Columns:

Nest variables (no empty columns)

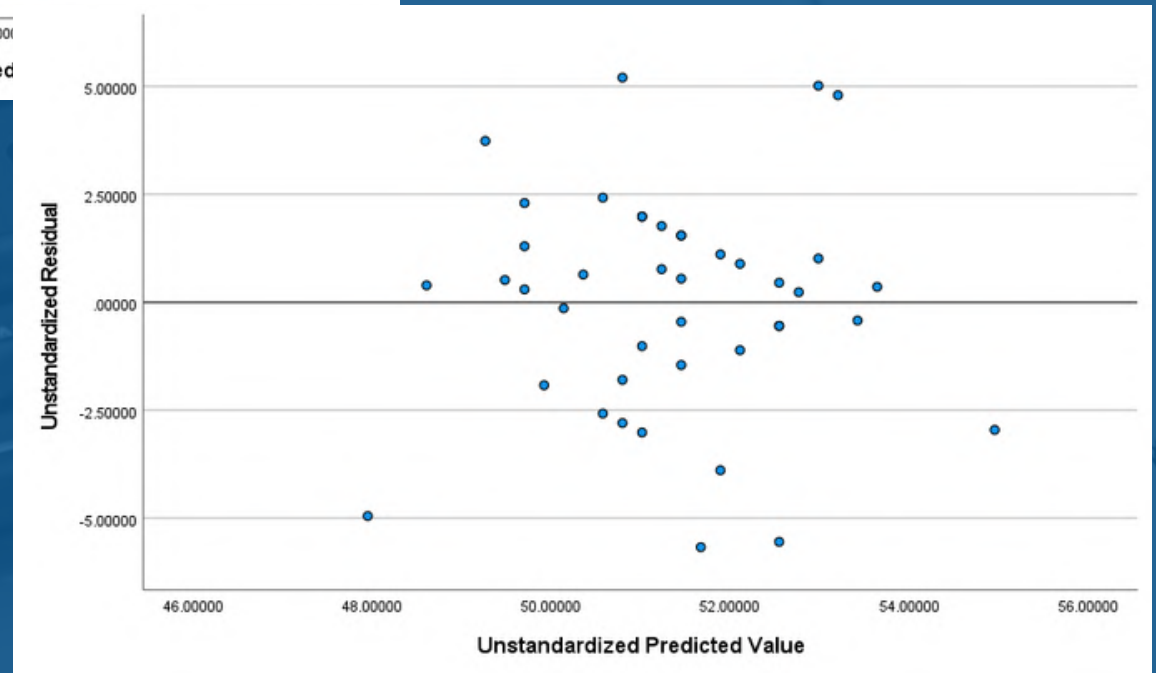
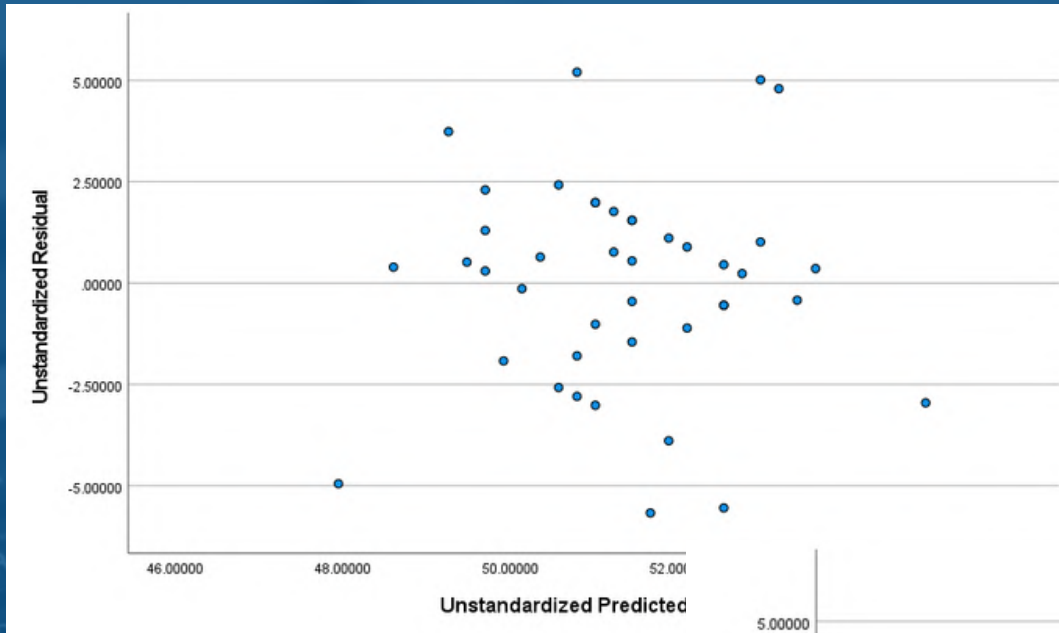
Template

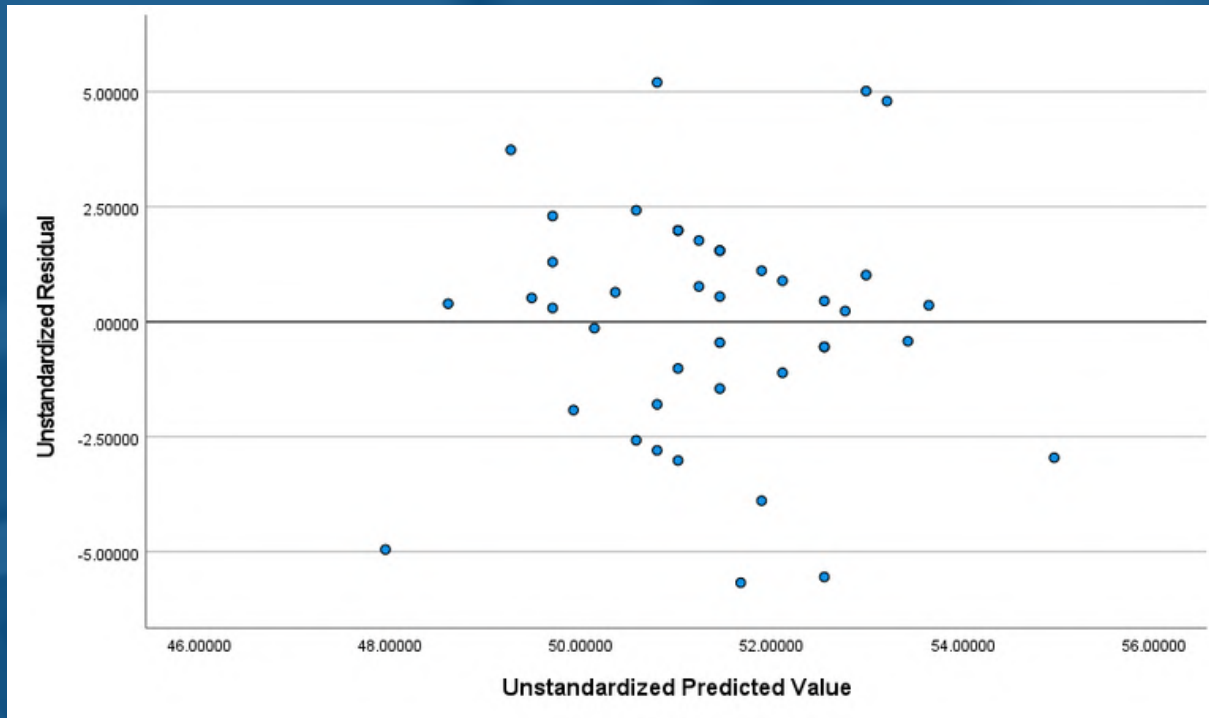
Use chart specifications from:
File...

OK **Paste** **Reset** **Cancel** **Help**

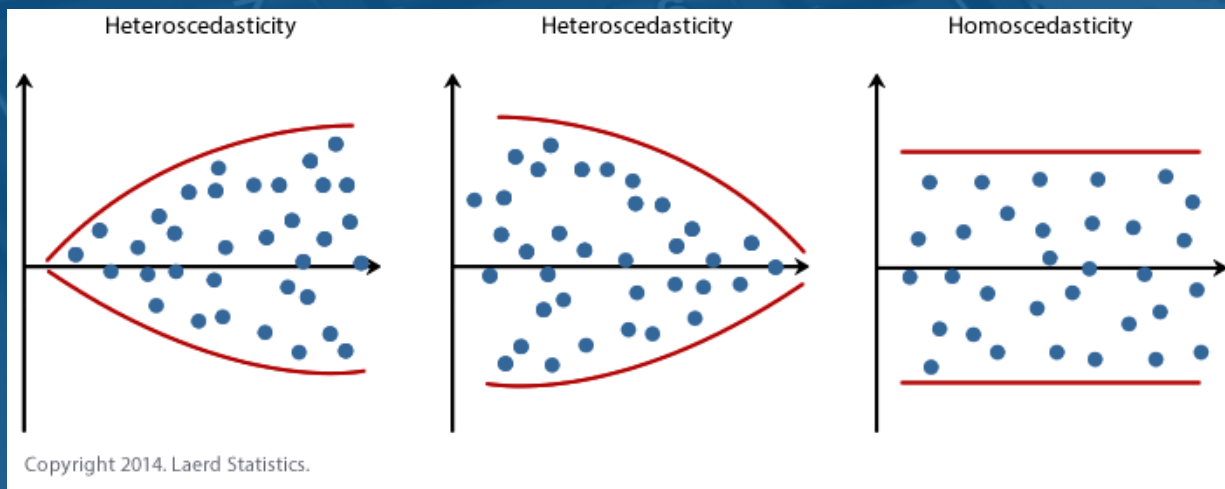
XP - YR

Double click the plot and click





There is no pattern in the scatter.
Homoscedasticity assumption is met.



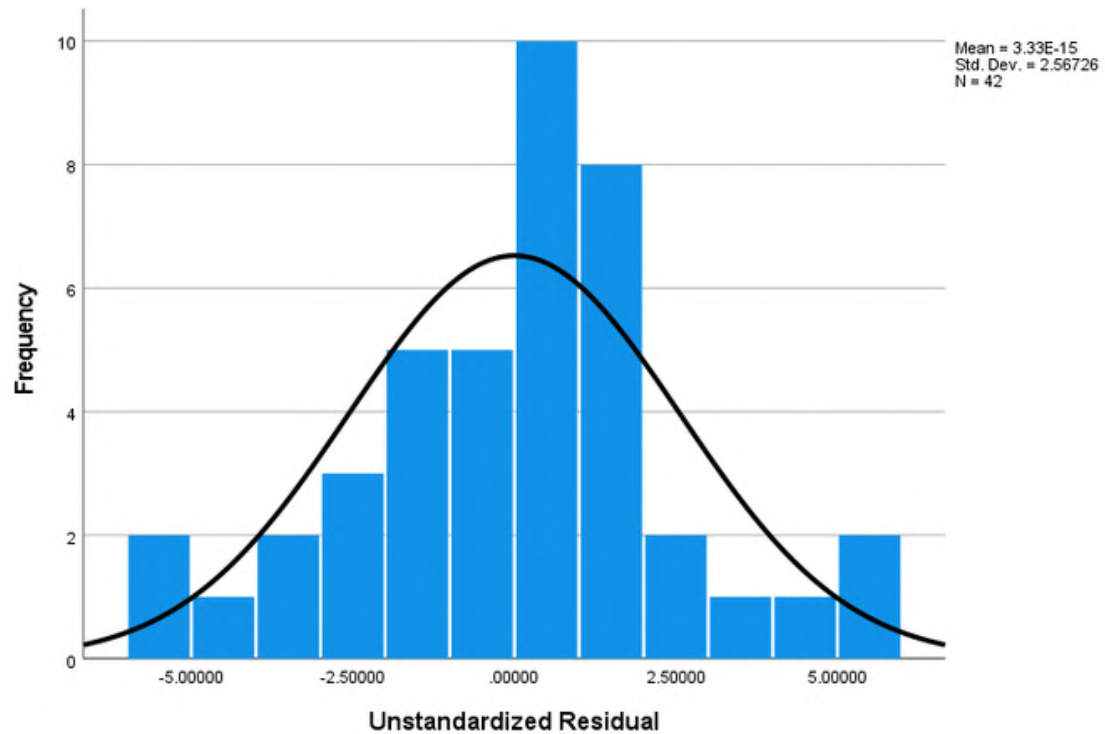
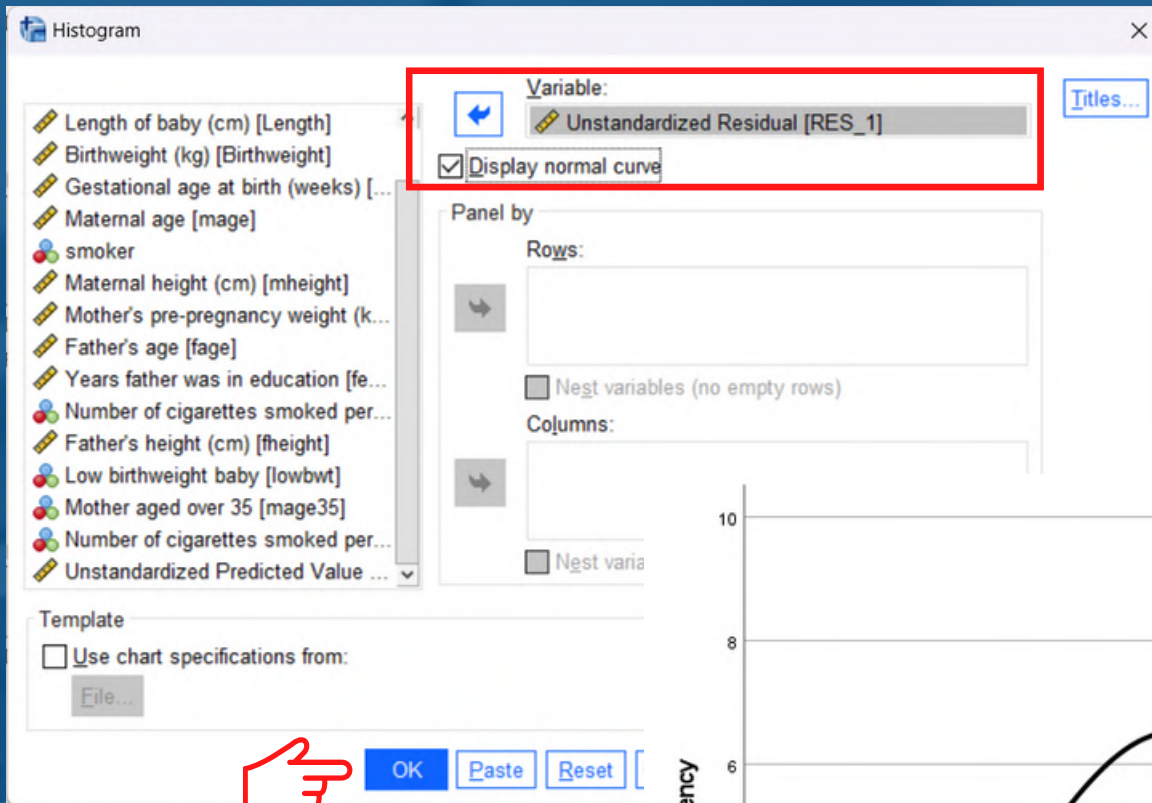
Example of heteroscedasticity and homoscedasticity

Checking assumption: Normality distribution of residuals

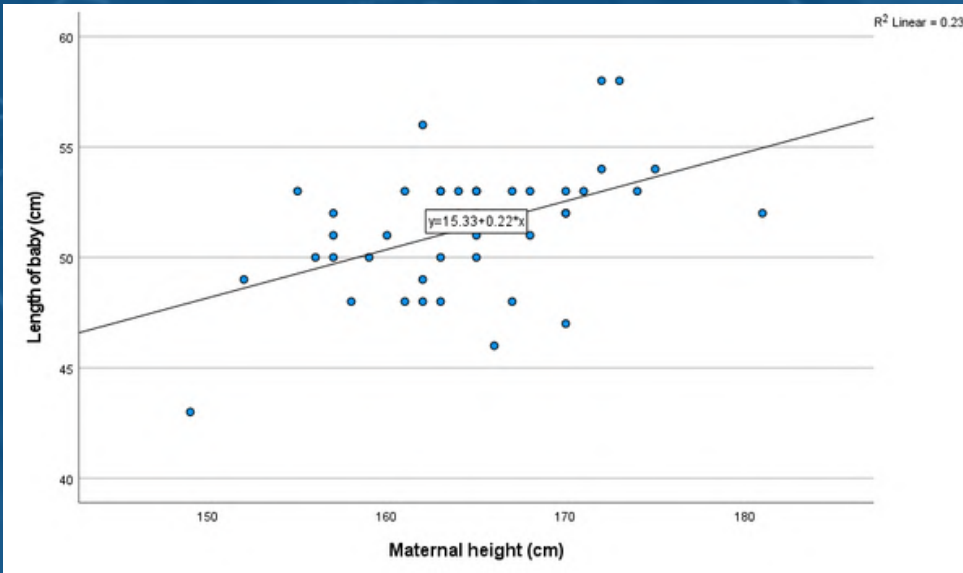
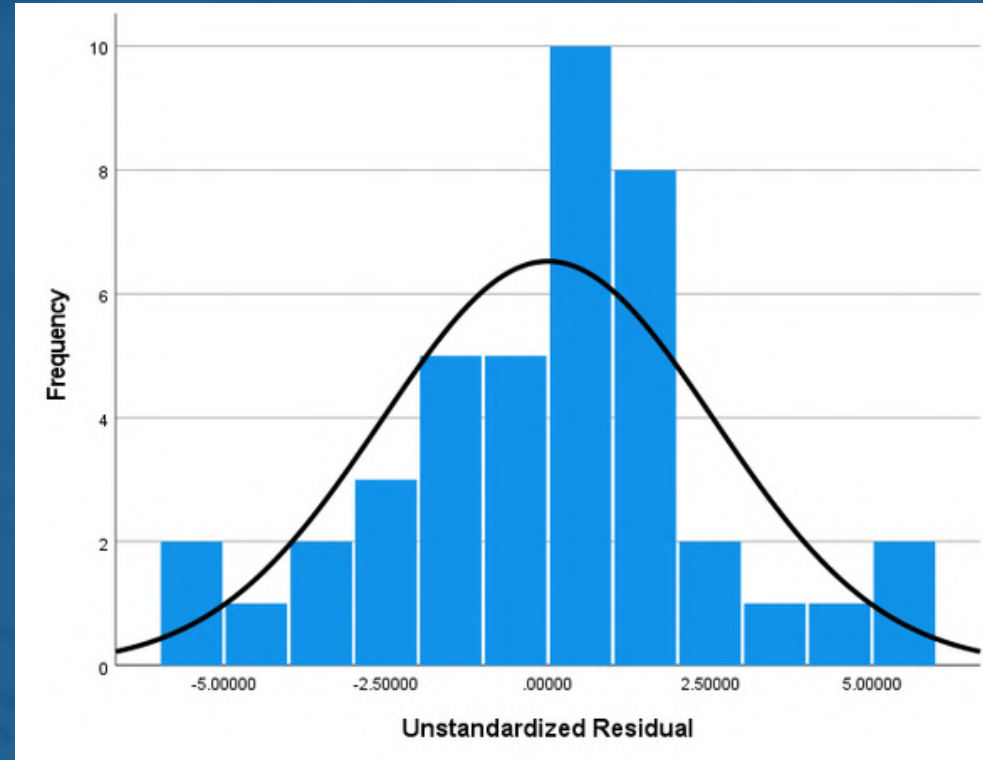
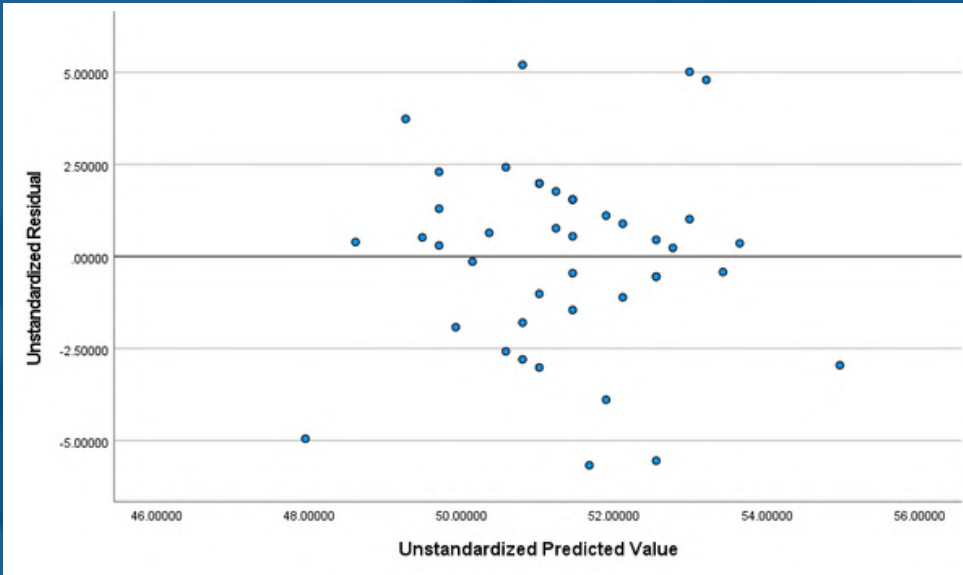
Go to: Graphs > Legacy Dialogs > Histogram

The screenshot shows the Minitab software interface. The 'Graphs' menu is open, and the path 'Legacy Dialogs' > 'Histogram...' is highlighted. A red hand icon points to the 'Legacy Dialogs' option, and another red hand icon points to the 'Histogram...' option. The background shows a calculator and a document with handwritten notes.

Row	Value	Normality Test
53	4.07	Non-s
54	3.94	Non-s
51	3.93	Non-s
52	3.77	Non-s
53	3.65	Non-s
54	3.63	Non-s
50	3.42	Non-s
53	3.35	Non-s
51	3.27	Non-s
52	3.23	Non-s
53	3.20	Non-s
53	3.15	Non-s
48	3.11	Non-s
48	3.03	Non-s



Residuals are normally distributed. Assumption is met.



Assumptions for homoscedasticity, linearity and normally distributed are met.

Step 4: Result Interpretation & Conclusion

Model	Unstandardized Coefficients		Standardized Coefficients	t	Sig.	95.0% Confidence Interval for B		
	B	Std. Error	Beta			Lower Bound	Upper Bound	
1	(Constant)	15.334	10.271		1.493	.143	-5.425	36.093
	Maternal height (cm)	.219	.062	.485	3.507	.001	.093	.345

a. Dependent Variable: Length of baby (cm)

Interpretation:

Increasing the mother's height by 1 cm will result in a 0.2 cm increase in the length of the baby (b=0.22, 95% CI 0.09, 0.35, p=0.001).

Regression equation:

$$y = a + bx$$

$$\text{length of baby} = 15.33 + (0.22 * \text{mother's height})$$

REGRESSION ANALYSIS



DEPENDENT VARIABLE	INDEPENDENT VARIABLE	STATISTICAL TEST
Numerical	Numerical	Multiple Linear Regression
Categorical (dichotomous)	Numerical and categorical	Multiple/Binary Logistic Regression
Categorical (polytomous - nominal)	Numerical and categorical	Multinomial Logistic Regression
Categorical (ordinal)	Numerical and categorical	Ordinal Logistic Regression



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**THANK
YOU**

The background of the slide is a blurred image of a computer monitor displaying financial data. On the left, there's a blue semi-transparent box containing the title and author's name. The monitor shows several windows: a 'Quote List (2)' window with columns for 'Name', 'Last', and 'Change'; a 'World Markets' window with a table of market indices; and several line charts showing price movements for various assets like EURUSD and Gold. The charts are overlaid on a grid, and the overall scene is dimly lit, focusing on the data presented on the screen.

PREDICTING THE FUTURE: INTRODUCTION TO REGRESSION ANALYSIS

NURULJANNAH BT NOR AZMI

MULTIPLE LINEAR REGRESSION

Multiple linear regression is used to estimate the relationship between **two or more independent variables** and **one dependent variable**.

Dependent (outcome) : numerical

Independent (predictor) : 2 or more numerical variables



MULTIPLE LINEAR REGRESSION

If independent variables are combination of numerical and categorical or categorical only -
General Linear Regression

Dependent (outcome) : numerical

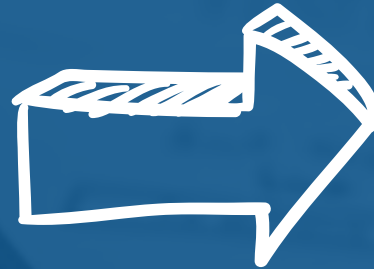
Independent (predictor) : 2 or more combination of numerical and categorical or categorical only



SIMPLE LINEAR REGRESSION - ONLY ONE INDEPENDENT VARIABLE

Independent variable (x)

Mother's height



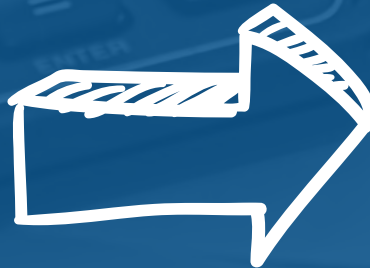
Dependent variable (y)

Length of baby

MULTIPLE LINEAR REGRESSION - MORE THAN ONE INDEPENDENT VARIABLES

Independent variables (x)

Mother's height
Mother's weight
Age



Dependent variable (y)

Length of baby

Multiple Linear Regression Model

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \dots + \beta_n X_n$$

Y = outcome

β_0 = intercept

$\beta_1 \dots \beta_n$ = regression coefficient for independent variable

$X_1 \dots X_n$ = independent variable

STEPS IN MULTIPLE LINEAR REGRESSION

1 Descriptive statistics

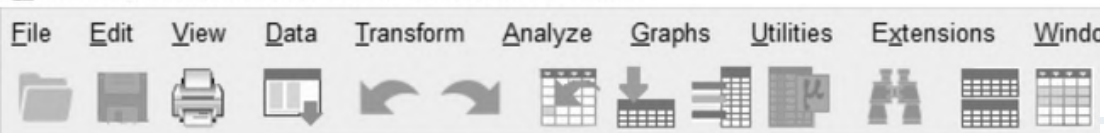
2 Simple linear regression (Univariable analysis)

3 Multiple linear regression (Multivariable analysis)

4 Checking multicollinearity & interaction (Preliminary final model)

5 Checking assumptions (final model)

6 Interpretation & presentation



9 :

	ID	Headcirc	Length	Birthweight	Ges
1	1360	34	56	4.55	
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4	1187	38	53	4.07	
5	553	37	54	3.94	
6	1636	38	51	3.93	
7	820	34	52	3.77	
8	1191	33	53	3.65	
9	1081	38	54	3.63	
10	822	35	50	3.42	
11	1683	33	53	3.35	
12	1088	36	51	3.27	
13	1107	36	52	3.23	
14	755	33	53	3.20	
15	1058	34	53	3.15	
16					
17					
18					
19					
20					
21					
22					
23					
24					
25					
26					
27	431	30	46	1.92	

EXAMPLE

Open dataset:
birthweight.sav

This dataset contains information on new born babies and their parents admitted in HKL. A researcher wants to determine the factors that are associated with the length of baby.

EXAMPLE

RQ: What are the factors that associated with the length of baby?

Length of baby (DV)

Factors (IV)

- Mother's age
- Mother's height
- Mother's weight

List down all the variables

Numerical

Numerical

Identify the types of variables

Multiple Linear Regression

Identify the right statistical analysis

STEP 1: DESCRIPTIVE STATISTICS

1. Data exploration and cleaning.
2. For categorical data, run the data by using Frequencies in SPSS.
3. For numerical data, run the data by using Descriptives/Explore in SPSS.

STEP 2: SIMPLE LINEAR REGRESSION (UNIVARIABLE ANALYSIS)

1. Do Simple Linear Regression analysis for each independent variable:

- Mother's age
- Mother's height
- Mother's weight

2. At the end, choose variables with p-value < 0.25 and/or clinically important.

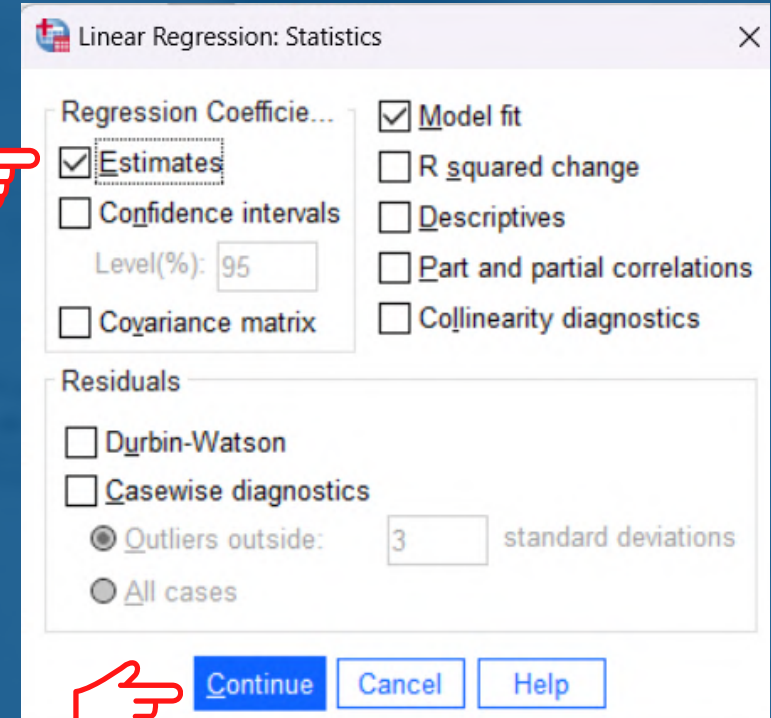
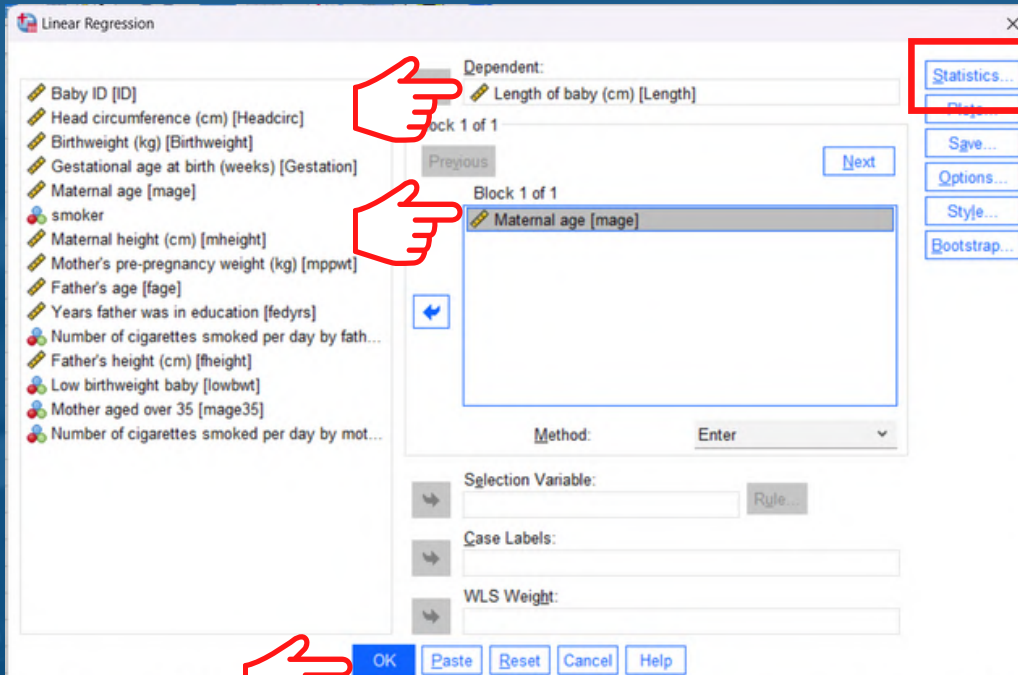
Go to: Analyze > Regression > Linear

The screenshot shows the IBM SPSS Statistics Data Editor interface. The 'Analyze' menu is open, and the 'Regression' option is selected. A sub-menu is displayed, showing 'Linear...' as the first option. Two red arrows point to the 'Regression' option in the main menu and the 'Linear...' option in the sub-menu.

ID	Head	Gestation	mage	sr
1	1360			
2	1016			
3	462			
4	1187			
5	553			
6	1636			
7	820			
8	1191			
9	1081			
10	822			
11	1683			
12	1088			
13	1107			
14	755			
15	1058			
16	321			
17	697			
18	808			
19	1600			
20	1313			
21	792			
22	1388			
23	575			
24	569			
25	1363			
26	300			
27	431			

Gestation	mage	sr
44	20	Non
40	19	Non
41	35	Non
44	20	Non
42	24	Non
38	29	Non
40	24	Non
37	20	
35	41	
33	20	

Length of baby vs Mother's age



Coefficients^a

Model		Unstandardized Coefficients		Standardized	t	Sig.	95.0% Confidence Interval for B	
		B	Std. Error	Beta			Lower Bound	Upper Bound
1	(Constant)	60.461	1.400		43.182	<.001	57.631	63.291
	Maternal age	-.318	.048	-.727	-6.691	<.001	-.414	-.222

a. Dependent Variable: Length of baby (cm)

There is a significant relationship between mother's age and the length of baby.

Length of baby vs Mother's height

Linear Regression

Dependent: Length of baby (cm) [Length]

Block 1 of 1

Maternal height (cm) [mheight]

Method: Enter

OK Paste Reset Cancel Help

Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.	95.0% Confidence Interval for B	
		B	Std. Error	Beta			Lower Bound	Upper Bound
1	(Constant)	15.334	10.271		1.493	.143	-5.425	36.093
	Maternal height (cm)	.219	.062	.485	3.507	.001	.093	.345

a. Dependent Variable: Length of baby (cm)



There is a significant relationship between mother's height and the length of baby.

Length of baby vs Mother's weight

Linear Regression

Dependent: Length of baby (cm) [Length]

Block 1 of 1

Block 1 of 1

Mother's pre-pregnancy weight (kg) [mppwt]

Method: Enter

Selection Variable: Rule...

Case Labels:

WLS Weight:

OK Paste Reset Cancel Help

Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.	95.0% Confidence Interval for B	
		B	Std. Error	Beta			Lower Bound	Upper Bound
1	(Constant)	41.996	3.427		12.255	<.001	35.070	48.922
	Mother's pre-pregnancy weight (kg)	.162	.059	.398	2.745	.009	.043	.282

a. Dependent Variable: Length of baby (cm)



There is a significant relationship between mother's pre-pregnancy weight and the length of baby.

Table 1: Associated factors of the length of baby by Simple Linear Regression

Variable	Simple Linear Regression	
	b* (95% CI)	p-value
Mother's age	-0.32 (-0.41,-0.22)	<0.001
Mother's height (cm)	0.22 (0.09,0.35)	0.001
Mother's pre-pregnancy weight (kg)	0.16 (0.04,0.28)	0.009

STEP 3: MULTIPLE LINEAR REGRESSION (MULTIVARIABLE ANALYSIS)

1. Variables selection can be done by using following methods:

- Forward
- Backward
- Stepwise

2. Perform all the methods and select the model with all variables significant as the preliminary main effect model.

STEP 4: CHECKING MULTICOLLINEARITY

1. Multicollinearity occurs when independent variables in a regression model are correlated.
2. This correlation is a problem because independent variables should be independent.
3. If the degree of correlation between variables is high enough, it can cause problems when you fit the model and interpret the results.
4. There is a high chance of getting inaccurate p-values and wide confidence interval of regression coefficient.

STEP 4: CHECKING MULTICOLLINEARITY





5. Multicollinearity can be checked by using Variance Inflation Factor (VIF).

6. If VIF is more than 10, then there is a multicollinearity amongst independent variables.

STEP 4: CHECKING INTERACTION

1. An interaction effect occurs when the effect of one variable depends on the value of another variable.
2. The interaction terms need to be biologically meaningful.
3. The interaction term needs to be computed in SPSS and then added to the model as an independent variable. If you have more than one interaction term, add to the model one by one.
4. If the interaction term is statistically significant, include the term in the model.

STEP 5: CHECKING ASSUMPTIONS

Assumptions	How to check?
1. <u>Independent</u> observation	Done during design stage
2. Overall <u>linearity</u>	Scatter plot between residuals and predicted values (XP - YR) 
3. Homoscedasticity (<u>Equal</u> variances)	Scatter plot between residuals and predicted values (XP - YR) 
4. <u>Linearity</u> of each independent variable	Scatter plot residual vs each independent variable (XI - YR) 
5. Residuals should be approximately <u>normally</u> distributed	Histogram with overlaid normal curve of residuals 

STEP 6: INTERPRETATION AND PRESENTATION

Coefficients^a

Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.	95.0% Confidence Interval for B	
		B	Std. Error	Beta			Lower Bound	Upper Bound
1	(Constant)	35.959	8.019		4.484	<.001	19.738	52.180
	Maternal age	-.282	.045	-.644	-6.303	<.001	-.372	-.191
	Maternal height (cm)	.143	.046	.316	3.094	.004	.049	.236

a. Dependent Variable: Length of baby (cm)

Run the final model. All the assumptions were checked and MET.

STEP 6: INTERPRETATION AND PRESENTATION

Table 2: Factors associated with the length of baby (n=42)

Variable	Simple Linear Regression		Multiple Linear Regression	
	b ^a (95% CI)	p-value	b ^b (95% CI)	p-value
Mother's age	-0.32 (-0.41,-0.22)	<0.001	-0.28 (-0.37,-0.19)	<0.001
Mother's height (cm)	0.22 (0.09,0.35)	0.001	0.14 (0.05,0.24)	0.004
Mother's pre-pregnancy weight (kg)	0.16 (0.04,0.28)	0.009	-	-

^a Crude regression coefficient

^b Adjusted regression coefficient

All model assumptions are fulfilled.

No multicollinearity problem detected and there were no interaction among the independent variables.

Coefficient of determination (R^2) = 0.621

Final model equation:

Length of baby = 35.96 – (0.28*mother's age) + (0.14*mother's height)

STEP 6: INTERPRETATION AND PRESENTATION

- There is a significant linear negative relationship between mother's age and the length of baby. For every one-year increase in the mother's age, the baby's length is 0.28 cm lower. (adjusted $b = -0.28$; 95% CI $-0.37, -0.19$; $p < 0.001$)
- There is a significant linear positive relationship between mother's height and the length of baby. For every 1 cm increase in the mother's height, the baby's length increases by 0.14 cm. (adjusted $b = 0.14$; 95% CI $0.05, 0.24$; $p = 0.004$)
- 62.1% of the variation in the length of baby is explained by mother's age and height according to the multiple linear regression model ($R = 0.621$).

REGRESSION ANALYSIS



DEPENDENT VARIABLE	INDEPENDENT VARIABLE	STATISTICAL TEST
Numerical	Numerical	Multiple Linear Regression
Categorical (dichotomous)	Numerical and categorical	Multiple/Binary Logistic Regression
Categorical (polytomous - nominal)	Numerical and categorical	Multinomial Logistic Regression
Categorical (ordinal)	Numerical and categorical	Ordinal Logistic Regression



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**THANK
YOU**